ALBERUNI'S INDIA.

AN ACCOUNT OF THE RELIGION, PHILOSOPHY, LITERATURE, GEOGRAPHY, CHRONOLOGY, ASTRONOMY, CUSTOMS, LAWS AND ASTROLOGY OF INDIA ABOUT A.D. 1030.

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An English Edition, with Notes and Indices.

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ALBÊRÛNÎ'S INDIA.

CHAPTER XLIX.

A SUMMARY DESCRIPTION OF THE ERAS.

THE eras serve to fix certain moments of time which are mentioned in some historical or astronomical connection. The Hindus do not consider it wearisome to reckon with huge numbers, but rather enjoy it. Still, in practical use, they are compelled to replace them by smaller (more handy) ones. Page 203. Enumeration of some of the eras of the Hindus.

Of their eras we mention—

1. The beginning of the existence of Brahman.

2. The beginning of the day of the present nychthemeron of Brahman, *i.e.* the beginning of the *kalpa*.

3. The beginning of the seventh *manvantara*, in which we are now.

4. The beginning of the twenty-eighth *caturyuga*, in which we are now.

5. The beginning of the fourth *yuga* of the present *caturyuga*, called *kalikâla*, *i.e.* the time of Kali. The whole *yuga* is called after him, though, accurately speaking, *his* time falls only in the last part of the *yuga*. Notwithstanding, the Hindus mean by *kalikâla* the beginning of the *kaliyuga*.

6. *Pâṇḍava-kâla*, *i.e.* the time of the life and the wars of Bhârata.

All these eras vie with each other in antiquity, the

one going back to a still more remote beginning than the other, and the sums of years which they afford go beyond hundreds, thousands, and higher orders of numbers. Therefore not only astronomers, but also other people, think it wearisome and unpractical to use them.

The author adopts the year 400 of Yazdajird as a test-year.

In order to give an idea of these eras, we shall use as a first gauge or point of comparison that Hindu year the great bulk of which coincides with the *year 400 of Yazdajird*. This number consists only of hundreds, not of units and tens, and by this peculiarity it is distinguished from all other years that might possibly be chosen. Besides, it is a memorable time; for the breaking of the strongest pillar of the religion, the decease of the pattern of a prince, Mahmûd, the lion of the world, the wonder of his time—may God have mercy upon him!—took place only a short time, less than a year, before it. The Hindu year precedes the Nauröz or new year's day of this year only by twelve days, and the death of the prince occurred precisely ten complete Persian months before it.

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Now, presupposing this our gauge as known, we shall compute the years for this point of junction, which is the beginning of the corresponding Hindu year, for the end of all years which come into question coincides with it, and the Nauröz of the year 400 of Yazdajird falls only a little latter (viz. twelve days).

How much of the life of Brahman has elapsed according to the *Vishṇu-Dharma*.

The book *Vishṇu-Dharma* says: "Vajra asked Mârkṣṇḍeya how much of the life of Brahman had elapsed; whereupon the sage answered: 'That which has elapsed is 8 years, 5 months, 4 days, 6 *manvantaras*, 7 *saṁdhi*, 27 *caturyugas*, and 3 *yugas* of the twenty-eighth *caturyuga*, and 10 *divya-years* up to the time of the *aśvamedha* which thou hast offered.' He who knows the details of this statement and comprehends them duly is a *sage* man, and *the sage* is he who serves the only Lord and strives to reach the neighbourhood of his place, which is called *Paramapada*."

Presupposing this statement to be known, and referring the reader to our explanation of the various measures of time which we have given in former chapters, we offer the following analysis.

Of the life of Brahman there have elapsed before our gauge 26,215,732,948,132 of our years. Of the nychthemeron of Brahman, *i.e.* of the *kalpa of the day*, there have elapsed 1,972,948,132, and of the seventh *manvantara* 120,532,132.

The latter is also the date of the imprisoning of the King Bali, for it happened in the first *caturyuga* of the seventh *manvantara*.

In all chronological dates which we have mentioned already and shall still mention, we only reckon with *complete* years, for the Hindus are in the habit of disregarding *fractions* of a year.

The time of Râma according to *Vishnu-Dharma*.

Further, the *Vishṇu-Dharma* says: "Mârkaṇḍeya says, in answer to a question of Vajra, 'I have already lived as long as 6 *kalpas* and 6 *manvantaras* of the seventh *kalpa*, 23 *tretâyugas* of the seventh *manvantara*. In the twenty-fourth *tretâyuga* Râma killed Râvaṇa, and Lakshmaṇa, the brother of Râma, killed Kumbhakarṇa, the brother of Râvaṇa. The two subjugated all the Râkshasas. At that time Vâlmiki, the Ṛishi, composed the story of Râma and Râmâyaṇa and eternalised it in his books. It was I who told it to Yudhishṭhira, the son of Pâṇḍu, in the forest of Kâmyakavana.'"

The author of the *Vishṇu-Dharma* reckons here with *tretâyugas*, first, because the events which he mentions occurred in a certain *tretâyuga*, and secondly, because it is more convenient to reckon with a simple unit than with such a unit as requires to be explained by reference to its single quarters. Besides, the latter part of the *tretâyuga* is a more suitable time for the events mentioned than its beginning, because it is so much nearer to the age of evil-doing (v. i. pp. 379, 380). No doubt, the date of Râma and Râmâyaṇa is known among the

Hindus, but I for my part have not been able to ascertain it.

Twenty-three *caturyugas* are 99,360,000 years, and, together with the time from the beginning of a *caturyuga* till the end of the *tretâyuga*, 102,384,000 years.

If we subtract this number of years from the number of years of the seventh *manvantara* that have elapsed before our gauge-year, viz. 120,532,132 (v. p. 3), we get the remainder of 18,148,132 years, *i.e.* so many years before our gauge-year as the conjectural date of Râma; and this may suffice, as long as it is not supported by a trustworthy tradition. The here-mentioned year corresponds to the 3,892,132d year of the 28th *caturyuga*.

How much time has elapsed before o of the present *kalpa*, according to Pulisa and Brahmagupta.

All these computations rest on the measures adopted by Brahmagupta. He and Pulisa agree in this, that the number of *kalpas* which have elapsed of the life of Brahman before the present *kalpa* is 6068 (equal to 8 years, 5 months, 4 days of Brahman). But they differ from each other in converting this number into *caturyugas*. According to Pulisa, it is equal to 6,116,544; according to Brahmagupta, only to 6,068,000 *caturyugas*. Therefore, if we adopt the system of Pulisa, reckoning 1 *manvantara* as 72 *caturyugas* without *sandhi*, 1 *kalpa* as 1008 *caturyugas*, and each *yuga* as the fourth part of a *caturyuga*, that which has elapsed of the life of Brahman before our gauge-year is the sum of 26,425,456,204,132 (!) years, and of the *kalpa* there have elapsed 1,986,124,132 years, of the *manvantara* 119,884,132 years, and of the *caturyuga* 3,244,132 years.

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How much time has elapsed of the current *kaliyuga*.

Regarding the time which has elapsed since the beginning of the *kaliyuga*, there exists no difference amounting to whole years. According to both Brahmagupta and Pulisa, of the *kaliyuga* there have elapsed before our gauge-year 4132 years, and between the

wars of Bhârata and our gauge-year there have elapsed 3479 years. The year 4132 before the gauge-year is the epoch of the *kalikâla*, and the year 3479 before the gauge-year is the epoch of the *Pâṇḍavakâla*.

The Hindus have an era called *Kâlayavana*, regarding which I have not been able to obtain full information. They place its epoch in the end of the last *dvâparayuga*. The here-mentioned Yavana (JMN) severely oppressed both their country and their religion. The era Kâlayavana.

To date by the here-mentioned eras requires in any case vast numbers, since their epochs go back to a most remote antiquity. For this reason people have given up using them, and have adopted instead the eras of—

(1.) *Śrî Harsha.*
(2.) *Vikramâditya.*
(3.) *Śaka.*
(4.) *Valabha*, and
(5.) *Gupta.*

The Hindus believe regarding Śrî Harsha that he used to examine the soil in order to see what of hidden treasures was in its interior, as far down as the seventh earth; that, in fact, he found such treasures; and that, in consequence, he could dispense with oppressing his subjects (by taxes, &c.) His era is used in Mathurâ and the country of Kanoj. Between Śrî Harsha and Vikramâditya there is an interval of 400 years, as I have been told by some of the inhabitants of that region. However, in the Kashmîrian calendar I have read that Śrî Harsha was 664 years later than Vikramâditya. In face of this discrepancy I am in perfect uncertainty, which to the present moment has not yet been cleared up by any trustworthy information. Era of Śrî Harsha.

Those who use the era of Vikramâditya live in the southern and western parts of India. It is used in the following way: 342 are multiplied by 3, which gives Era of Vikramâditya.

the product 1026. To this number you add the years which have elapsed of the current *shashṭyabda* or sexagesimal *samvatsara*, and the sum is the corresponding year of the era of Vikramâditya. In the book *Srâdhava* by Mahâdeva I find as his name *Candrabîja*.

As regards this method of calculation, we must first say that it is rather awkward and unnatural, for if they began with 1026 as the basis of the calculation, as they begin—without any apparent necessity—with 342, this would serve the same purpose. And, secondly, admitting that the method is correct as long as there is only *one shashṭyabda* in the date, how are we to reckon if there is a number of *shashṭyabdas*?

The Śaka-kâla.

The epoch of the era of Śaka or Śakakâla falls 135 years later than that of Vikramâditya. The here-mentioned Śaka tyrannised over their country between the river Sindh and the ocean, after he had made Âryavarta in the midst of this realm his dwelling-place. He interdicted the Hindus from considering and representing themselves as anything but Śakas. Some maintain that he was a Śûdra from the city of Almanṣûra; others maintain that he was not a Hindu at all, and that he had come to India from the west. The Hindus had much to suffer from him, till at last they received help from the east, when Vikramâditya marched against him, put him to flight and killed him in the region of Karûr, between Multân and the castle of Lônî. Now this date became famous, as people rejoiced in the news of the death of the tyrant, and was used as the epoch of an era, especially by the astronomers. They honour the conqueror by adding Śrî to his name, so as to say Śrî Vikramâditya. Since there is a long interval between the era which is called the era of Vikramâditya (v. p. 5) and the killing of Śaka, we think that that Vikramâditya from whom the era has got its name is not identical with that one who killed Śaka, but only a namesake of his.

The era of Valabha is called so from Valabha, the ruler of the town Valabhî, nearly 30 *yojanas* south of Anhilvâra. The epoch of this era falls 241 years later than the epoch of the Śaka era. People use it in this way. They first put down the year of the Śakakâla, and then subtract from it the cube of 6 and the square of 5 (216 + 25 = 241). The remainder is the year of the Valabha era. The history of Valabha is given in its proper place (cf. chap. xvii.) Era of Valabha. Page 206.

As regards the Guptakâla, people say that the Guptas were wicked powerful people, and that when they ceased to exist this date was used as the epoch of an era. It seems that Valabha was the last of them, because the epoch of the era of the Guptas falls, like that of the Valabha era, 241 years later than the Śakakâla. Guptakâla.

The *era of the astronomers* begins 587 years later than the Śakakâla. On this era is based the canon *Khaṇḍakhâdyaka* by Brahmagupta, which among Muhammadans is known as *Al-arkand*. Era of the astronomers.

Now, the year 400 of Yazdajird, which we have chosen as a gauge, corresponds to the following years of the Indian eras:— Comparison of the epochs of the Indian eras with the test-year.

(1) To the year 1488 of the era of Śrî Harsha,
(2) To the year 1088 of the era of Vikramâditya,
(3) To the year 953 of the Śakakâla,
(4) To the year 712 of the Valabha era, which is identical with the Guptakâla,
(5) To the year 366 of the era of the canon *Khaṇḍakhâdyaka*,
(6) To the year 526 of the era of the canon *Pañcasiddhântikâ* by Varâhamihira,
(7) To the year 132 of the era of the canon *Karaṇasâra*; and
(8) To the year 65 of the era of the canon *Karaṇatilaka*.

The eras of the here-mentioned *canones* are such as the authors of them considered the most suitable to be used as cardinal points in astronomical and other calculations, whence calculation may conveniently extend forward or backward. Perhaps the epochs of these eras fall within the time when the authors in question themselves lived, but it is also possible that they fall within a time anterior to their lifetime.

On the popular mode of dating by centennia or samvatsaras.

Common people in India date by the years of a *centennium*, which they call *samvatsara*. If a *centennium* is finished, they drop it, and simply begin to date by a new one. This era is called *lokakâla*, *i.e.* the era of the nation at large. But of this era people give such totally different accounts, that I have no means of making out the truth. In a similar manner they also differ among themselves regarding the beginning of the year. On the latter subject I shall communicate what I have heard myself, hoping meanwhile that one day we shall be able to discover a rule in this apparent confusion.

Different beginnings of the year.

Those who use the Śaka era, the astronomers, begin the year with the month Caitra, whilst the inhabitants of Kanîr, which is conterminous with Kashmîr, begin it with the month Bhâdrapada. The same people count our gauge-year (400 Yazdajird) as the eighty-fourth year of an era of theirs.

All the people who inhabit the country between Bardarî and Mârîgala begin the year with the month Kârttika, and they count the gauge-year as the 110th year of an era of theirs. The author of the Kashmirian calendar maintains that the latter year corresponds to the sixth year of a new *centennium*, and this, indeed, is the usage of the people of Kashmîr.

The people living in the country Nîrahara, behind Mârîgala, as far as the utmost frontiers of Tâkeshar and Lohâvar, begin the year with the month Mârgaśîrsha, and reckon our gauge-year as the 108th year of their

era. The people of *Lanbaga, i.e.* Lamghân, follow their example. I have been told by people of Multân that this system is peculiar to the people of Sindh and Kanoj, and that they used to begin the year with the new moon of Mârgaśirsha, but that the people of Multân only a few years ago had given up this system, and had adopted the system of the people of Kashmîr, and followed their example in beginning the year with the new moon of Caitra.

Popular mode of dating in use among the Hindus, and criticisms thereon.

I have already before excused myself on account of the imperfection of the information given in this chapter. For we cannot offer a strictly scientific account of the eras to which it is devoted, simply because in them we have to reckon with periods of time far exceeding a *centennium*, (and because all tradition of events farther back than a hundred years is confused (v. p. 8).) So I have myself seen the roundabout way in which they compute the year of the destruction of Somanâth in the year of the Hijra 416, or 947 Śakakâla. First, they write down the number 242, then under it 606, then under this 99. The sum of these numbers is 947, or the year of the Śakakâla.

Now I am inclined to think that the 242 years have elapsed before the beginning of their centennial system, and that they have adopted the latter together with the Guptakâla; further, that the number 606 represents complete *samvatsaras* or centennials, each of which they must reckon as 101 years; lastly, that the 99 years represent that time which has elapsed of the current *centennium*.

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That this, indeed, is the nature of the calculation is confirmed by a leaf of a canon composed by Durlabha of Multân, which I have found by chance. Here the author says: "First write 848 and add to it the *laukika-kâla, i.e.* the era of the people, and the sum is the Śakakâla."

If we write first the year of the Śakakâla correspond-

ing to our gauge-year, viz. 953, and subtract 848 from it, the remainder, 105, is the year of the *laukika-kâla*, whilst the destruction of Somanâth falls in the ninety-eighth year of the *centennium* or *laukika-kâla*.

Durlabha says, besides, that the year begins with the month Mârgaśîrsha, but that the astronomers of Multân begin it with Caitra.

Origin of the dynasty of the Shâhs of Kâbul.

The Hindus had kings residing in Kâbul, Turks who were said to be of Tibetan origin. The first of them, Barhatakîn, came into the country and entered a cave in Kâbul, which none could enter except by creeping on hands and knees. The cave had water, and besides he deposited there victuals for a certain number of days. It is still known in our time, and is called *Var*. People who consider the name of Barhatakîn as a good omen enter the cave and bring out some of its water with great trouble.

Certain troops of peasants were working before the door of the cave. Tricks of this kind can only be carried out and become notorious, if their author has made a secret arrangement with somebody else — in fact, with confederates. Now these had induced persons to work there continually day and night in turns, so that the place was never empty of people.

Some days after he had entered the cave, he began to creep out of it in the presence of the people, who looked on him as a new-born baby. He wore Turkish dress, a short tunic open in front, a high hat, boots and arms. Now people honoured him as a being of miraculous origin, who had been destined to be king, and in fact he brought those countries under his sway and ruled them under the title of a *shâhiya of Kâbul*. The rule remained among his descendants for generations, the number of which is said to be about sixty.

Unfortunately the Hindus do not pay much attention to the historical order of things, they are very careless

in relating the chronological succession of their kings, and when they are pressed for information and are at a loss, not knowing what to say, they invariably take to tale-telling. But for this, we should communicate to the reader the traditions which we have received from some people among them. I have been told that the pedigree of this royal family, written on silk, exists in the fortress *Nagarkot*, and I much desired to make myself acquainted with it, but the thing was impossible for various reasons.

The story of Kanik.

One of this series of kings was Kanik, the same who is said to have built the *vihâra* (Buddhistic monastery) of Purushâvar. It is called, after him, *Kanik-caitya*. People relate that the king of Kanoj had presented to him, among other gifts, a gorgeous and most singular piece of cloth. Now Kanik wanted to have dresses made out of it for himself, but his tailor had not the courage to make them, for he said, "There is (in the embroidery) the figure of a human foot, and whatever trouble I may take, the foot will always lie between the shoulders." And that means the same as we have already mentioned in the story of Bali, the son of Virocana (*i.e.* a sign of subjugation, cf. i. p. 397). Now Kanik felt convinced that the ruler of Kanoj had thereby intended to vilify and disgrace him, and in hot haste he set out with his troops marching against him.

When the *rât* heard this, he was greatly perplexed, for he had no power to resist Kanik. Therefore he consulted his Vazîr, and the latter said, "You have roused a man who was quiet before, and have done unbecoming things. Now cut off my nose and lips, let me be mutilated, that I may find a cunning device; for there is no possibility of an open resistance." The *rât* did with him as he had proposed, and then he went off to the frontiers of the realm.

There he was found by the hostile army, was recognised and brought before Kanik, who asked what was the matter with him. The Vazir said, "I tried to dissuade *him* from opposing you, and sincerely advised him to be obedient to you. He, however, conceived a suspicion against me and ordered me to be mutilated. Since then he has gone, of his own accord, to a place which a man can only reach by a very long journey when he marches on the highroad, but which he may easily reach by undergoing the trouble of crossing an intervening desert, supposing that he can carry with himself water for so and so many days." Thereupon Kanik answered: "The latter is easily done." He ordered water to be carried along, and engaged the Vazir to show him the road. The Vazir marched before the king and led him into a boundless desert. After the number of days had elapsed and the road did not come to an end, the king asked the Vazir what was now to be done. Then the Vazir said, "No blame attaches to me that I tried to save my master and to destroy his enemy. The nearest road leading out of this desert is that on which you have come. Now do with me as you like, for none will leave this desert alive."

Then Kanik got on his horse and rode round a depression in the soil. In the centre of it he thrust his spear into the earth, and lo! water poured from it in sufficient quantity for the army to drink from and to draw from for the march back. Upon this the Vazir said, "I had not directed my cunning scheme against powerful angels, but against feeble men. As things stand thus, accept my intercession for the prince, my benefactor, and pardon him." Kanik answered, "I
Page 208. march back from this place. Thy wish is granted to thee. Thy master has already received what is due to him." Kanik returned out of the desert, and the Vazir went back to his master, the *rái* of Kanoj. There he

found that on the same day when Kanik had thrust his spear into the earth, both the hands and feet had fallen off the body of the *rât*.

End of the Tibetan dynasty, and origin of the Brahman dynasty.

The last king of this race was *Lagatûrmân*, and his Vazîr was Kallar, a Brahman. The latter had been fortunate, in so far as he had found by accident hidden treasures, which gave him much influence and power. In consequence, the last king of this Tibetan house, after it had held the royal power for so long a period, let it by degrees slip from his hands. Besides, Lagatûrmân had bad manners and a worse behaviour, on account of which people complained of him greatly to the Vazîr. Now the Vazîr put him in chains and imprisoned him for correction, but then he himself found ruling sweet, his riches enabled him to carry out his plans, and so he occupied the royal throne. After him ruled the Brahman kings Sâmand (Sâmanta), Kamalû, Bhîm (Bhîma), Jaipâl (Jayapâla), Ânandapâla, Tarojanapâla (Trilocanapâla). The latter was killed A.H. 412 (A.D. 1021), and his son Bhîmapâla five years later (A.D. 1026).

This Hindu Shâhiya dynasty is now extinct, and of the whole house there is no longer the slightest remnant in existence. We must say that, in all their grandeur, they never slackened in the ardent desire of doing that which is good and right, that they were men of noble sentiment and noble bearing. I admire the following passage in a letter of Ânandapâla, which he wrote to the prince Maḥmûd, when the relations between them were already strained to the utmost: "I have learned that the Turks have rebelled against you and are spreading in Khurâsân. If you wish, I shall come to you with 5000 horsemen, 10,000 foot-soldiers, and 100 elephants, or, if you wish, I shall send you my son with double the number. In acting thus, I do not speculate on the impression which this will make on you. I have been conquered by *you*, and

therefore I do not wish that another man should conquer you."

The same prince cherished the bitterest hatred against the Muhammadans from the time when his son was made a prisoner, whilst his son Tarojanapâla (Trilocanapâla) was the very opposite of his father.

CHAPTER I.

HOW MANY STAR-CYCLES THERE ARE BOTH IN A "KALPA" AND IN A "CATURYUGA."

It is one of the conditions of a *kalpa* that in it the planets, with their apsidea and nodes, must unite in 0° of Aries, *i.e.* in the point of the vernal equinox. Therefore each planet makes within a *kalpa* a certain number of complete revolutions or cycles.

The tradition of Alfazârî and Ya'ḳûb Ibn Ṭârik.

These star-cycles as known through *the canon* of Alfazârî and Ya'ḳûb Ibn Ṭârik, were derived from a Hindu who came to Bagdad as a member of the political mission which Sindh sent to the Khalif Almanṣûr, A.H. 154 (=A.D. 771). If we compare these secondary statements with the primary statements of the Hindus, we discover discrepancies, the cause of which is not known to me. Is their origin due to the translation of Alfazârî and Ya'ḳûb? or to the dictation of that Hindu? or to the fact that afterwards these computations have been corrected by Brahmagupta, or some one else? For, certainly, any scholar who becomes aware of mistakes in astronomical computations and takes an interest in the subject, will endeavour to correct them, as, *e.g.* Muḥammad Ibn Isḥâḳ of Sarakhs has done. For he had discovered in the computation of Saturn a falling back behind real time (*i.e.*, that Saturn, according to this computation, revolved slower than it did in reality). Now he assiduously studied the subject, till at last he was convinced that his fault did not originate

Muḥammad Ibn Isḥâḳ of Sarakhs.

from the *equation* (i.e. from the correction of the places of the stars, the computation of their mean places). Then he added to the cycles of Saturn one cycle more, and compared his calculation with the actual motion of the planet, till at last he found the calculation of the cycles completely to agree with astronomical observation. In accordance with this correction he states the star-cycles in his *canon*.

Âryabhaṭa quoted by Brahmagupta.

Brahmagupta relates a different theory regarding the cycles of the apsides and nodes of the moon, on the authority of Âryabhaṭa. We quote this from Brahmagupta, for we could not read it in the original work of Âryabhaṭa, but only in a quotation in the work of Brahmagupta.

Number of the rotations of the planets in a kalpa. Page 209.

The following table contains all these traditions, which will facilitate the study of them, if God will!

The planets.	Number of their revolutions in a Kalpa.	Number of the revolutions of their apsides.	Number of the revolutions of their nodes.
Sun	4,320,000,000	480	Has no node.
Moon. Brahmagupta	57,753,300,000	488,105,858	232,311,168
Moon. The translation of Alfazârî			232,312,138
Moon. Âryabhaṭa		488,219,000	232,316,000
Moon. The anomalistic revolution of the moon according to Brahmagupta		57,765,194,142	The anomalistic revolution of the moon is here treated as if it were the apsis, being the difference between the motion of the moon and that of the apsis. (See the *notes*.)
Mars	2,296,828,522	292	267
Mercury	17,936,998,984	332	521
Jupiter	364,226,455	855	63
Venus	7,022,389,492	653	893
Saturn. Brahmagupta	146,567,298	41	584
Saturn. The translation of Alfazârî	146,569,284		
Saturn. The correction of Alsarakhsî	146,569,238		
The fixed stars	120,000 according to the translation of Alfazârî.		

The computation of these cycles rests on the mean motion of the planets. As a *caturyuga* is, according to Brahmagupta, the one-thousandth part of a *kalpa*, we have only to divide these cycles by 1000, and the quotient is the number of the star-cycles in one *caturyuga*. Cycles of the planets in a *caturyuga* and *kaliyuga*.

Likewise, if we divide the cycles of the table by 10,000, the quotient is the number of the star-cycles in a *kaliyuga*, for this is one-tenth of a *caturyuga*. The fractions which may occur in those quotients are raised to wholes, to *caturyugas* or *kaliyugas*, by being multiplied by a number equal to the denominator of the fraction.

The following table represents the star-cycles specially in a *caturyuga* and *kaliyuga*, not those in a *manvantara*. Although the *manvantaras* are nothing but multiplications of whole *caturyugas*, still it is difficult to reckon with them on account of the *sandhi* which is attached both to the beginning and to the end of them.

The names of the planets.	Their revolutions in a Caturyuga.	Their revolutions in a Kaliyuga.
Sun	4,320,000	432,000
His apsis	$0\frac{1}{4}$	$0\frac{60}{1000}$
Moon	57,753,300	5,775,330
Her apsis: Brahmagupta	$488,105\frac{420}{1000}$	$48,810\frac{2420}{1000}$
Her apsis: Aryabhata	488,219	$48,821\frac{9}{10}$
Her anomalistic revolution	$57,265,194\frac{11}{1000}$	$5,726,519\frac{2071}{2000}$
Her node: Brahmagupta	$232,311\frac{21}{125}$	$23,231\frac{289}{2500}$
Her node: The translation of Alfazari	$232,312\frac{50}{1000}$	$23,231\frac{1668}{1000}$
Her node: Aryabhata	232,316	$23,231\frac{3}{5}$
Mars	$2,296,828\frac{461}{1000}$	$229,682\frac{4461}{5000}$
His apsis	$0\frac{75}{1000}$	$0\frac{750}{1000}$
His node	$0\frac{2207}{10000}$	$0\frac{2207}{10000}$
Mercury	$17,936,998\frac{123}{125}$	$1,793,699\frac{1123}{1250}$
His apsis	$0\frac{83}{360}$	$0\frac{830}{3600}$
His node	$0\frac{521}{1000}$	$0\frac{5211}{10000}$
Jupiter	$364,226\frac{61}{100}$	$36,422\frac{1261}{2000}$
His apsis	$0\frac{171}{400}$	$0\frac{1711}{4000}$
His node	$0\frac{62}{1000}$	$0\frac{63}{10000}$

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The names of the planets.	Their revolutions in a Caturyuga.	Their revolutions in a Kaliyuga.
Venus	7,022,389	702,238
Her apsis	488	488
Her node	232	232
Saturn	146,567	14,656
His apsis	964	964
His node	364	364
Saturn { The translation of Alfazârî	146,569	14,656
Saturn { The correction of Alsarakhsî	146,569	14,656
The fixed stars	120	12

Page 211. Star-cycles of a kalpa and caturyuga, according to Pulisa.

After we have stated how many of the star-cycles of a *kalpa* fall in a *caturyuga* and in a *kaliyuga*, according to Brahmagupta, we shall now derive from the number of star-cycles of a *caturyuga* according to Pulisa the number of star-cycles of a *kalpa*, first reckoning a *kalpa* = 1000 *caturyugas*, and, secondly, reckoning it as 1008 *caturyugas*. These numbers are contained in the following table:—

The Yugas according to Pulisa.

The names of the 9 planets.	Number of their revolutions in a Caturyuga.	Number of their revolutions in a Kalpa of 1000 Caturyugas.	Number of their revolutions in a Kalpa of 1008 Caturyugas.
Sun	4,320,000	4,320,000,000	4,354,560,000
Moon	57,753,336	57,753,336,000	58,215,362,688
Her apsis	488,219	488,219,000	492,124,752
Her node	232,226	232,226,000	234,083,808
Mars	2,296,824	2,296,824,000	2,315,198,592
Mercury	17,937,000	17,937,000,000	18,080,496,000
Jupiter	364,220	364,220,000	367,133,760
Venus	7,022,388	7,022,388,000	7,078,567,104
Saturn	146,564	146,564,000	147,736,512

Transformation of the word Āryabhaṭa among the Arabs.

We meet in this context with a curious circumstance. Evidently Alfazârî and Ya'ḳûb sometimes heard from their Hindu master expressions to this effect, that his calculation of the star-cycles was that of *the great Siddhânta, whilst Āryabhaṭa reckoned with one-thousandth*

part of it. They apparently did not understand him properly, and imagined that *âryabhaṭa* (Arab. *ârjabhad*) meant *a thousandth part.* The Hindus pronounce the *ḍ* of this word something between a *d* and an *r*. So the consonant became changed to an *r*, and people wrote *ârjabhar.* Afterwards it was still more mutilated, the first *r* being changed to a *z*, and so people wrote *âzjabhar.* If the word in this garb wanders back to the Hindus, they will not recognise it.

Star-cycles according to Abû-alḥasan of Al'ahwâz.

Further, Abû-alḥasan of Al'ahwâz mentions the revolutions of the planets in *the years of al-arjabhar, i.e.* in *caturyugas.* I shall represent them in the table such as I have found them, for I guess that they are directly derived from the dictation of that Hindu. Possibly, therefore, they give us the theory of Âryabhaṭa. Some of these numbers agree with the star-cycles in a *caturyuga,* which we have mentioned on the authority of Brahmagupta; others differ from them, and agree with the theory of Pulisa; and a third class of numbers differs from those of both Brahmagupta and Pulisa, as the examination of the whole table will show.

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The names of the planets.	Their Yugas as parts of a Caturyuga according to Abû-alḥasan Al'ahwâz.
Sun	4,320,000
Moon	57,753,336
Her apsis . .	488,219
Her node . .	232,226
Mars	2,296,828
Mercury . . .	17,937,020
Jupiter . . .	364,224
Venus	7,022,388
Saturn . . .	146,564

CHAPTER LI.

AN EXPLANATION OF THE TERMS "ADHIMÂSA," "ÛNA-RÂTRA," AND THE "AHARGAṆAS," AS REPRESENTING DIFFERENT SUMS OF DAYS.

On the leap month.

THE months of the Hindus are lunar, their years solar; therefore their new year's day must in each solar year fall by so much earlier as the lunar year is shorter than the solar (roughly speaking, by eleven days). If this precession makes up one complete month, they act in the same way as the Jews, who make the year a leap year of thirteen months by reckoning the month Adar twice, and in a similar way to the heathen Arabs, who in a so-called *annus procrastinationis* postponed the new year's day, thereby extending the preceding year to the duration of thirteen months.

The Hindus call the year in which a month is repeated in the common language *malamâsa*. *Mala* means the dirt that clings to the hand. As such dirt is thrown away, thus the leap month is thrown away out of the calculation, and the number of the months of a year remains twelve. However, in the literature the leap month is called *adhimâsa*.

That month is repeated within which (it being considered as a solar month) two lunar months finish. If the end of the lunar month coincides with the beginning of the solar month, if, in fact, the former ends before any part of the latter has elapsed, this month is repeated, because the end of the lunar month, although

it has not yet run into the new solar month, still does no longer form part of the preceding month.

If a month is repeated, the first time it has its ordinary name, whilst the second time they add before the name the word *durâ* to distinguish between them. If, *e.g.* the month Âshâḍha is repeated, the first is called Âshâḍha, the second *Durâshâḍha*. The first month is that which is disregarded in the calculation. The Hindus consider it as unlucky, and do not celebrate any of the festivals in it which they celebrate in the other months. The most unlucky time in this month is that day on which the lunation reaches its end. Page 213.

The author of the *Vishṇu-Dharma* says: "*Candra* (*mâna*) is smaller than *sâvana*, *i.e.* the lunar year is smaller than the civil year, by six days, *i.e. ûnarâtra*. *Ûna* means *decrease, deficiency*. *Saura* is greater than *candra* by eleven days, which gives in two years and seven months the supernumerary *adhimâsa* month. This whole month is unlucky, and nothing must be done in it." Quotation from the *Vishṇu-Dharma*.

This is a rough description of the matter. We shall now describe it accurately.

The lunar year has 360 lunar days, the solar year has $371\frac{31}{180}$ lunar days. This difference sums up to the thirty days of an *adhimâsa* in the course of $976\frac{4176}{17709}$ lunar days, *i.e.* in 32 months, or in 2 years, 8 months, 16 days, *plus* the fraction: $\frac{4176}{17709}$ lunar day, which is nearly = 5 minutes, 15 seconds.

As the religious reason of this theory of intercalation the Hindus mention a passage of the *Veda*, which they have read to us, to the following tenor: "If the day of conjunction, *i.e.* the first lunar day of the month, passes without the sun's marching from one zodiacal sign to the other, and if this takes place on the following day, the preceding month falls out of the calculation." Quotation from the *Veda*.

The meaning of this passage is not correct, and the fault must have risen with the man who recited and Criticisms thereon.

translated the passage to me. For a month has thirty lunar days, and a twelfth part of the solar year has $30\frac{11}{124}$ lunar days. This fraction, reckoned in day-minutes, is equal to $55^{\prime}\ 19^{\prime\prime}\ 22^{\prime\prime\prime}\ 30^{\prime\prime\prime}$. If we now, for example, suppose a conjunction or new moon to take place at 0° of a zodiacal sign, we add this fraction to the time of the conjunction, and thereby we find the times of the sun's entering the signs successively. As now the difference between a lunar and a solar month is only a fraction of a day, the sun's entering a new sign may naturally take place on any of the days of the month. It may even happen that the sun enters two consecutive signs on the same month-day (*e.g.* on the second or third of two consecutive months). This is the case if in one month the sun enters a sign before $4^{\prime}\ 40^{\prime\prime}\ 37^{\prime\prime\prime}\ 30^{\prime\prime\prime}$ have elapsed of it; for the next following entering a sign falls later by $55^{\prime}\ 19^{\prime\prime}\ 23^{\prime\prime\prime}\ 30^{\prime\prime\prime}$, and both these fractions (*i.e.* less than $4^{\prime}\ 40^{\prime\prime}\ 37^{\prime\prime\prime}\ 30^{\prime\prime\prime}$ *plus* the last-mentioned fraction) added together are not sufficient to make up one complete day. Therefore the quotation from the *Veda* is not correct.

Proposed explanation of the Vedic passage.

I suppose, however, that it may have the following correct meaning:—If a month elapses in which the sun does not march from one sign to another, this month is disregarded in the calculation. For if the sun enters a sign on the 29th of a month, when at least $4^{\prime}\ 40^{\prime\prime}\ 37^{\prime\prime\prime}\ 30^{\prime\prime\prime}$ have elapsed of it, this entering takes place before the beginning of the succeeding month, and therefore the latter month is without an entering of the sun into a new sign, because the next following entering falls on the first of the next but one or third month. If you compute the consecutive enterings, beginning with a conjunction taking place in 0° of a certain sign, you find that in the thirty-third month the sun enters a new sign at $30^{\prime}\ 20^{\prime\prime}$ of the twenty-ninth day, and that he enters the next following sign at $25^{\prime}\ 39^{\prime\prime}\ 22^{\prime\prime\prime}\ 30^{\prime\prime\prime}$ of the first day of the thirty-fifth month.

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Hence also becomes evident why this month, which is disregarded in the calculation, is considered as unlucky. The reason is that the month misses just that moment which is particularly adapted to earn in it a heavenly reward, viz. the moment of the sun's entering a new sign.

As regards *adhimâsa*, the word means *the first month*, for AD means *beginning* (*i.e. âdi*). In the books of Ya'ḳûb Ibn Ṭârik and of Alfazârî this name is written *padamâsa*. *Pada* (in the orig. *P–Dh*) means *end*, and it is possible that the Hindus call the leap month by both names; but the reader must be aware that these two authors frequently misspell or disfigure the Indian words, and that there is no reliance on their tradition. I only mention this because Pulisa explains the latter of the *two* months, which are called by the same name, as the supernumerary one.

Explanation of the terms *universal* or *partial* months and days.

The month, as the time from one conjunction to the following, is one revolution of the moon, which revolves through the ecliptic, but in a course distant from that of the sun. This is the difference between the motions of the two heavenly luminaries, whilst the direction in which they move is the same. If we subtract the revolutions of the sun, *i.e.* the solar cycles of a *kalpa*, from its lunar cycles, the remainder shows how many more lunar months a *kalpa* has than solar months. All months or days which we reckon as parts of whole *kalpas* we call here *universal*, and all months or days which we reckon as parts of a part of a *kalpa*, *e.g.* of a *caturyuga*, we call *partial*, for the purpose of simplifying the terminology.

Universal adhimâsa months.

The year has twelve solar months, and likewise twelve lunar months. The lunar year is complete with twelve months, whilst the solar year, in consequence of the difference of the two year kinds, has, with the addition of the *adhimâsa*, thirteen months. Now evidently the difference between the universal solar and

lunar months is represented by these supernumerary months, by which a single year is extended to thirteen months. These, therefore, are the *universal adhimâsa* months.

The *universal* solar months of a *kalpa* are 51,840,000,000; the *universal* lunar months of a *kalpa* are 53,433,300,000. The difference between them or the *adhimâsa* months is 1,593,300,000.

Multiplying each of these numbers by 30, we get days, viz. solar days of a *kalpa*, 1,555,200,000,000; lunar days, 1,602,999,000,000; the days of the *adhimâsa* months, 47,799,000,000.

In order to reduce these numbers to smaller ones we divide them by a common divisor, viz. 9,000,000. Thus we get as the sum of the days of the solar months 172,800; as the sum of the days of the lunar months, 178,111; and as the sum of the days of the *adhimâsa* months, 5311.

How many solar, lunar, and civil days are required for the formation of an adhimâsa month.

If we further divide the *universal solar*, *civil*, and *lunar* days of a *kalpa*, each kind of them separately, by the *universal adhimâsa* months, the quotient represents the number of days within which a whole *adhimâsa* month sums up, viz. in $976\frac{484}{1311}$ solar days, in $1006\frac{484}{1311}$ lunar days, and in $990\frac{3663}{10033}$ civil days.

This whole computation rests on the measures which Brahmagupta adopts regarding a *kalpa* and the star-cycles in a *kalpa*.

The computation of adhimâsa according to Pulisa. Page 215.

According to the theory of Pulisa regarding the *caturyuga*, a *caturyuga* has 51,840,000 solar months, 53,433,336 lunar months, 1,593,336 *adhimâsa* months. Accordingly a *caturyuga* has 1,555,200,000 solar days, 1,603,000,080 lunar days, 47,800,080 days of *adhimâsa* months.

If we reduce the numbers of the months by the common divisor of 24, we get 2,160,000 solar months, 2,226,389 lunar months, 66,389 *adhimâsa* months. If we divide the numbers of the day by the common

divisor of 720, we get 2,160,000 solar days, 2,226,389 lunar days, 66,389 days of the *adhimâsa* months. If we, lastly, divide the *universal* solar, lunar, and civil days of a *caturyuga*, each kind separately, by the universal *adhimâsa* months of a *caturyuga*, the quotient represents the numbers of days within which a whole *adhimâsa* month sums up, viz. in $976\frac{4336}{66389}$ solar days, in $1006\frac{4336}{66389}$ lunar days, and in $990\frac{21468}{66389}$ civil days.

These are the elements of the computation of the *adhimâsa*, which we have worked out for the benefit of the following investigations.

Explanation of the term *ûnarâtra*.

Regarding the cause which necessitates the *ûnarâtra*, lit. *the days of the decrease*, we have to consider the following.

If we have one year or a certain number of years, and reckon for each of them twelve months, we get the corresponding number of solar months, and by multiplying the latter by 30, the corresponding number of solar days. It is evident that the number of the lunar months or days of the same period is the same, *plus* an increase which forms one or several *adhimâsa* months. If we reduce this increase to *adhimâsa* months due to the period of time in question, according to the relation between the universal solar months and the universal *adhimâsa* months, and add this to the months or days of the years in question, the sum represents the *partial* lunar days, *i.e.* those which correspond to the given number of years.

This, however, is not what is wanted. What we want is the number of *civil* days of the given number of years which are *less* than the lunar days; for one *civil* day is greater than one *lunar* day. Therefore, in order to find that which is sought, we must subtract something from the number of lunar days, and this element which must be subtracted is called *ûnarâtra*.

The *ûnarâtra* of the *partial* lunar days stands in the same relation to the *universal* lunar days as the uni-

versal civil days are less than the universal lunar days. The universal lunar days of a *kalpa* are 1,602,999,000,000. This number is larger than the number of universal civil days by 25,082,550,000, which represents the universal *ûnarâtra*.

Both these numbers may be diminished by the common divisor of 450,000. Thus we get 3,562,220 universal lunar days, and 55,739 universal *ûnarâtra* days.

Computation of the ûnarâtra according to Pulisa.

According to Pulisa, a *caturyuga* has 1,603,000,080 lunar days, and 25,082,280 *ûnarâtra* days. The common divisor by which both numbers may be reduced is 360. Thus we get 4,452,778 lunar days and 69,673 *ûnarâtra* days.

These are the rules for the computation of the *ûnarâtra*, which we shall hereafter want for the computation of the *ahargaṇa*. The word means *sum of days*; for *ah* means *day*, and *argaṇa*, *sum*.

Criticisms on Ya'kûb Ibn Ṭârik.

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Ya'kûb Ibn Ṭârik has made a mistake in the computation of the solar days; for he maintains that you get them by subtracting the solar cycles of a *kalpa* from the civil days of a *kalpa*, *i.e.* the *universal* civil days. But this is not the case. We get the solar days by multiplying the solar cycles of a *kalpa* by 12, in order to reduce them to months, and the product by 30, in order to reduce them to days, or by multiplying the number of cycles by 360.

In the computation of the lunar days he has first taken the right course, multiplying the lunar months of a *kalpa* by 30, but afterwards he again falls into a mistake in the computation of the days of the *ûnarâtra*. For he maintains that you get them by subtracting the solar days from the lunar days, whilst the correct thing is to subtract the *civil* days from the lunar days.

CHAPTER LII.

ON THE CALCULATION OF "AHARGAṆA" IN GENERAL, THAT IS, THE RESOLUTION OF YEARS AND MONTHS INTO DAYS, AND, VICE VERSÂ, THE COMPOSITION OF YEARS AND MONTHS OUT OF DAYS.

General rule how to find the *ahargaṇa*.

THE general method of resolution is as follows:—The complete years are multiplied by 12; to the product are added the months which have elapsed of the current year, [and this sum is multiplied by 30;] to this product are added the days which have elapsed of the current month. The sum represents the *saurâhargaṇa*, *i.e.* the sum of the partial solar days.

You write down the number in two places. In the one place you multiply it by 5311, *i.e.* the number which represents the *universal adhimâsa* months. The product you divide by 172,800, *i.e.* the number which represents the *universal* solar months. The quotient you get, as far as it contains complete days, is added to the number in *the second place*, and the sum represents the *candrâhargaṇa*, *i.e.* the sum of the partial lunar days.

The latter number is again written down in two different places. In the one place you multiply it by 55,739, *i.e.* the number which represents the *universal tnarâtra* days, and divide the product by 3,562,220, *i.e.* the number which represents the universal lunar days. The quotient you get, as far as it represents complete days, is subtracted from the number written in the second place, and the remainder is the *sâvanâhargaṇa*, *i.e.* the sum of *civil* days which we wanted to find.

More detailed rule for the same purpose.

However, the reader must know that this computation applies to dates in which there are only complete *adhimâsa* and *ûnarâtra* days, without any fraction. If, therefore, a given number of years commences with the beginning of a *kalpa*, or a *caturyuga*, or a *kaliyuga*, this computation is correct. But if the given years begin with some other time, it may by chance happen that this computation is correct, but possibly, too, it may result in proving the existence of *adhimâsa* time, and in that case the computation would not be correct. Also the reverse of these two eventualities may take place. However, if it is known with what particular moment in the *kalpa*, *caturyuga*, or *kaliyuga* a given number of years commences, we use a special method of computation, which we shall hereafter illustrate by some examples.

The latter method carried out for Śaka-kâla 953.

We shall carry out this method for the beginning of the Indian year Śakakâla 953, the same year which we use as the gauge-year in all these computations.

First we compute the time from the beginning of the life of Brahman, according to the rules of Brahmagupta. We have already mentioned that 6068 *kalpas* have elapsed before the present one. Multiplying this by the well-known number of the days of a *kalpa* (1,577,916,450,000 civil days, *vide* i. p. 368), we get 9,574,797,018,600,000 as the sum of the days of 6068 *kalpas*.

Dividing this number by 7, we get 5 as a remainder, and reckoning five days backwards from the Saturday which is the last day of the preceding *kalpa*, we get Tuesday as the first day of the life of Brahman.

We have already mentioned the sum of the days of a *caturyuga* (1,577,916,450 days, v. i. p. 370), and have explained that a *kṛitayuga* is equal to four-tenths of it, *i.e.* 631,166,580 days. A *manvantara* has seventy-one times as much, *i.e.* 112,032,067,950 days. The days of

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six *manvantaras* and their *sandhi*, consisting of seven *kritayuga*, are 676,610,573,760. If we divide this number by 7, we get a remainder of 2. Therefore the six *manvantaras* end with a Monday, and the seventh begins with a Tuesday.

Of the seventh *manvantara* there have already elapsed twenty-seven *caturyugas*, *i.e.* 42,603,744,150 days. If we divide this number by 7, we get a remainder of 2. Therefore the twenty-eighth *caturyuga* begins with a Thursday.

The days of the *yugas* which have elapsed of the present *caturyuga* are 1,420,124,805. The division by 7 gives the remainder 1. Therefore the *kaliyuga* begins with a Friday.

Now, returning to our gauge-year, we remark that the years which have elapsed of the *kalpa* up to that year are 1,972,948,132. Multiplying them by 12, we get as the number of their months 23,675,377,584. In the date which we have adopted as gauge-year there is no month, but only complete years; therefore we have nothing to add to this number.

By multiplying this number by 30 we get days, viz. 710,261,327,520. As there are no days in the normal date, we have no days to add to this number. If, therefore, we had multiplied the number of years by 360, we should have got the same result, viz. the *partial* solar days.

Multiply this number by 5311 and divide the product by 172,800. The quotient is the number of the *adhimâsa* days, viz. $21,829,849,018\frac{103}{1250}$. If, in multiplying and dividing, we had used the months, we should have found the *adhimâsa* months, and, multiplied by 30, they would be equal to the here-mentioned number of *adhimâsa* days.

If we further add the *adhimâsa* days to the *partial* solar days, we get the sum of 732,091,176,538, *i.e.* the *partial* lunar days. Multiplying them by 55,739, and

dividing the product by 3,562,220, we get the *partial ûnarâtra* days, viz., $11,455,224,575\frac{1}{1}\frac{1}{1}\frac{1}{1}\frac{1}{1}\frac{1}{1}\frac{1}{1}$.

This sum of days without the fraction is subtracted from the *partial* lunar days, and the remainder, 720,635,951,963, represents the number of the *civil* days of our gauge-date.

Dividing it by 7, we get as remainder 4, which means that the last of these days is a Wednesday. Therefore the Indian year commences with a Thursday.

If we further want to find the *adhimâsa* time, we divide the *adhimâsa* days by 30, and the quotient is the number of the *adhimâsas* which have elapsed, viz. 727,661,633, *plus* a remainder of 28 days, 51 minutes, 30 seconds, for the current year. This is the time which has already elapsed of the *adhimâsa* month of the current year. To become a complete month, it only wants 1 day, 8 minutes, 30 seconds more.

The same calculation applied to a caturyuga according to the theory of Pulisa.

We have here used the solar and lunar days, the *adhimâsa* and *ûnarâtra* days, to find a certain past portion of a *kalpa*. We shall now do the same to find the past portion of a *caturyuga*, and we may use the same elements for the computation of a *caturyuga* which we have used for that of a *kalpa*, for both methods lead to the same result, as long as we adhere to one and the same theory (*e.g.* that of Brahmagupta), and do not mix up different chronological systems, and as long as each *guṇakâra* and its *bhâgabhâra*, which we here mention together, correspond to each other in the two computations.

The former term means a *multiplicator* in all kinds of calculations. In our (Arabic) astronomical handbooks, as well as those of the Persians, the word occurs in the form *gunc̣r*. The second term means each *divisor*. It occurs in the astronomical handbooks in the form *bahcâr*.

It would be useless if we were to exemplify this computation on a *caturyuga* according to the theory of Brah-

magupta, as according to him a *caturyuga* is simply one- Page 218.
thousandth of a *kalpa*. We should only have to shorten the above-mentioned numbers by three ciphers, and in every other respect get the same results. Therefore we shall now give this computation according to the theory of Pulisa, which, though applying to the *caturyuga*, is similar to the method of computation used for a *kalpa*.

According to Pulisa, in the moment of the beginning of the gauge-year, there have elapsed of the years of the *caturyuga* 3,244,132, which are equal to 1,167,887,520 solar days. If we multiply the number of months which corresponds to this number of days with the number of the *adhimâsa* months of a *caturyuga* or a corresponding multiplicator, and divide the product by the number of the solar months of a *caturyuga*, or a corresponding divisor, we get as the number of *adhimâsa* months $1,196,525\frac{446837}{1080000}$.

Further, the past 3,244,132 years of the *caturyuga* are 1,203,783,270 lunar days. Multiplying them by the number of the *ûnarâtra* days of a *caturyuga*, and dividing the product by the lunar days of a *caturyuga*, we get as the number of *ûnarâtra* days $18,835,700\frac{598,055}{1.2.3.385}$. Accordingly, the *civil* days which have elapsed since the beginning of the *caturyuga* are 1,184,947,570, and this it was which we wanted to find.

A similar method of computation taken from the *Pulisa-siddhânta*.

We shall here communicate a passage from the *Pulisa-siddhânta*, describing a similar method of computation, for the purpose of rendering the whole subject clearer to the mind of the reader, and fixing it there more thoroughly. Pulisa says: "We first mark the *kalpas* which have elapsed of the life of Brahman before the present *kalpa*, *i.e.* 6068. We multiply this number by the number of the *caturyugas* of a *kalpa*, *i.e.* 1008. Thus we get the product 6,116,544. This number we multiply by the number of the *yugas* of a *caturyuga*, *i.e.* 4, and get the product 24,466,176. This number we multiply by the number of years of a *yuga*,

i.e. 1,080,000, and get the product 26,423,470,080,000. These are the years which have elapsed before the present *kalpa*.

We further multiply the latter number by 12, so as to get months, viz. 317,081,640,960,000. We write down this number in two different places.

In the one place, we multiply it by the number of the *adhimâsa* months of a *caturyuga*, *i.e.* 1,593,336, or a corresponding number which has been mentioned in the preceding, and we divide the product by the number of the solar months of a *caturyuga*, *i.e.* 51,840,000. The quotient is the number of *adhimâsa* months, viz. 9,745,709,750,784.

This number we add to the number written in the second place, and get the sum of 326,827,350,710,784. Multiplying this number by 30, we get the product 9,804,820,521,323,520, viz. lunar days.

This number is again written down in two different places. In the one place we multiply it by the *ûnarâtra* of a *caturyuga*, *i.e.* the difference between civil and lunar days, and divide the product by the lunar days of a *caturyuga*. Thus we get as quotient 153,416,869,240,320, *i.e.* *ûnarâtra* days.

We subtract this number from that one written in the second place, and we get as remainder 9,651,403,652,083,200, *i.e.* the days which have elapsed of the life of Brahman before the present *kalpa*, or the days of 6068 *kalpas*, each *kalpa* having 1,590,541,142,400 days. Dividing this sum of days by 7, we get no remainder. This period of time ends with a Saturday, and the present *kalpa* commences with a *Sunday*. This shows that the beginning of the life of Brahman too was a Sunday.

Page 219. Of the current *kalpa* there have elapsed six *manvantaras*, each of 72 *caturyugas*, and each *caturyuga* of 4,320,000 years. Therefore six *manvantaras* have 1,866,240,000 years. This number we compute in the

same way as we have done in the preceding example. Thereby we find as the number of days of six complete *manvantaras*, 681,660,489,600. Dividing this number by 7, we get as remainder 6. Therefore the elapsed *manvantaras* end with a Friday, and the seventh *manvantara* begins with a *Saturday*.

Of the current *manvantara* there have elapsed 27 *caturyugas*, which, according to the preceding method of computation, represent the number of 42,603,780,600 days. The twenty-seventh *caturyuga* ends with a *Monday*, and the twenty-eighth begins with a Tuesday.

Of the current *caturyuga* there have elapsed three *yugas*, or 3,240,000 years. These represent, according to the preceding method of computation, the number of 1,183,438,350 days. Therefore these three *yugas* end with a Thursday, and *kaliyuga* commences with a Friday.

Accordingly, the sum of days which have elapsed of the *kalpa* is 725,447,708,550, and the sum of days which have elapsed between the beginning of the life of Brahman and the beginning of the present *kaliyuga* is 9,652,129,099,791,750.

The method of *akargaṇa* employed by Âryabhaṭa.

To judge from the quotations from Âryabhaṭa, as we have not seen a book of his, he seems to reckon in the following manner:—

The sum of days of a *caturyuga* is 1,577,917,500. The time between the beginning of the *kalpa* and the beginning of the *kaliyuga* is 725,447,570,625 days. The time between the beginning of the *kalpa* and our gauge-date is 725,449,079,845. The number of days which have elapsed of the life of Brahman before the present *kalpa* is 9,651,401,817,120,000.

This is the correct method for the resolution of years into days, and all other measures of time are to be treated in accordance with this.

We have already pointed out (on p. 26) a mistake

The elements as given by Ya'ḳûb Ibn Ṭârik.

of Ya'ḳûb Ibn Ṭârik in the calculation of the universal solar and *anardîra* days. As he translated from the Indian language a calculation the reasons of which he did not understand, it would have been his duty to examine it, and to check the various numbers of it one by the other. He mentions in his book also the method of *ahargaṇa*, *i.e.* the resolution of years, but his description is not correct; for he says:—

"Multiply the months of the given number of years by the number of the *adhimâsa* months which have elapsed up to the time in question, according to the well-known rules of *adhimâsa*. Divide the product by the solar months. The quotient is the number of complete *adhimâsa* months *plus* its fractions which have elapsed up to the date in question."

The mistake is here so evident that even a copyist would notice it; how much more a mathematician who makes a computation according to this method; for he multiplies by the *partial adhimâsa* instead of the *universal*.

A second method given by Ya'ḳûb.

Besides, Ya'ḳûb mentions in his book another and perfectly correct method of resolution, which is this: "When you have found the number of months of the years, multiply them by the number of the lunar months, and divide the product by the solar months. The quotient is the number of *adhimâsa* months together with the number of the months of the years in question.

"This number you multiply by 30, and you add to the product the days which have elapsed of the current month. The sum represents the lunar days.

"If, instead of this, the first number of months were multiplied by 30, and the past portion of the month were added to the product, the sum would represent the partial solar days; and if this number were further computed according to the preceding method, we should get the *adhimâsa* days together with the solar days."

The rationale of this calculation is the following:—If we multiply, as we have done, by the number of the universal *adhimâsa* months, and divide the product by the universal solar months, the quotient represents the portion of *adhimâsa* time by which we have multiplied. As, now, the lunar months are the sum of solar and *adhimâsa* months, we multiply by them (the lunar months) and the division remains the same. The quotient is the sum of that number which is multiplied and that one which is sought for, *i.e.* the lunar days. Explication of the last-mentioned method.

We have already mentioned in the preceding part that by multiplying the lunar days by the universal *ûnarâtra* days, and by dividing the product by the universal lunar days, we get the portion of *ûnarâtra* days which belongs to the number of lunar days in question. However, the *civil* days in a *kalpa* are less than the lunar days by the amount of the *ûnarâtra* days. Now the lunar days we have stand in the same relation to the lunar days *minus* their due portion of *ûnarâtra* days as the whole number of lunar days (of a *kalpa*) to the whole number of lunar days (of a *kalpa*) *minus* the complete number of *ûnarâtra* days (of a *kalpa*); and the latter number are the *universal civil* days. If we, therefore, multiply the number of lunar days we have by the universal civil days, and divide the product by the universal lunar days, we get as quotient the number of civil days of the date in question, and that it was which we wanted to find. Instead of multiplying by the whole sum of civil days (of a *kalpa*), we multiply by 3,506,481, and instead of dividing by the whole number of lunar days (of a *kalpa*), we divide by 3,562,220. Page 220.

The Hindus have still another method of calculation. It is the following:—"They multiply the elapsed years of the *kalpa* by 12, and add to the product the complete months which have elapsed of the current year. The sum they write down above the number 69,120, Another method of *âharyaṇa* of the Hindus.

(*Lacuna.*)

and the number they get is subtracted from the number written down in the middle place. The double of the remainder they divide by 65. Then the quotient represents the partial *adhimâsa* months. This number they add to that one which is written down in the uppermost place. They multiply the sum by 30, and add to the product the days which have elapsed of the current month. The sum represents the partial solar days. This number is written down in two different places, one under the other. They multiply the lower number by 11, and write the product under it. Then they divide it by 403,963, and add the quotient to the middle number. They divide the sum by 703, and the quotient represents the partial *ûnarâtra* days. This number they subtract from the number written in the uppermost place, and the remainder is the number of civil days which we want to find."

Explication of the latter method.

The rationale of this computation is the following:—If we divide the universal solar months by the universal *adhimâsa* months, we get as the measure of one *adhimâsa* month $32\frac{8844}{12533}$ solar months. The double of this is $65\frac{11155}{12533}$ solar months. If we divide by this number the double of the months of the given years, the quotient is the number of the partial *adhimâsas*. However, if we divide by wholes *plus* a fraction, and want to subtract from the number which is divided a certain portion, the remainder being divided by the wholes only, and the two subtracted portions being equal portions of the wholes to which they belong, the whole divisor stands in the same relation to its fraction as the divided number to the subtracted portion.

The latter method applied to the gauge-year.

If we make this computation for our gauge-year, we get the fraction of $\frac{11155}{1.036.800}$, and dividing both numbers by 15, we get $\frac{7\,7}{69120}$.

It would also be possible here to reckon by single *adhimâsas* instead of double ones, and in that case it

would not be necessary to double the remainder. But the inventor of this method seems to have preferred the reduplication in order to get smaller numbers; for if we reckon with single *adhimâsas*, we get the fraction of $\frac{8844}{518400}$, which may be reduced by 96 as a common divisor. Thereby we get 89 as the multiplicator, and 5400 as the divisor. In this the inventor of the method has shown his sagacity, for the reason for his computation is the intention of getting partial lunar days and smaller multiplicators.

His method (*i.e.* Brahmagupta's) for the computation of the *ûnarâtra* days is the following:— Method for the computation of the *ûnarâtra* days according to Brahmagupta. Page 221.

If we divide the universal lunar days by the universal *ûnarâtra* days, we get as quotient 63 and a fraction, which may be reduced by the common divisor 450,000. Thus we get $63\frac{150.653}{353.739}$ lunar days as the period of time within which one *ûnarâtra* day sums up. If we change this fraction into eleventh parts, we get $\frac{0}{11}$ and a remainder of $\frac{45.842}{353.739}$, which, if expressed in minutes, is equal to 0′ 59″ 54‴.

Since this fraction is very near to one whole, people have neglected it, and use, in a rough way, $\frac{10}{11}$ instead. Therefore, according to the Hindus, one *ûnarâtra* day sums up in $63\frac{10}{11}$ or $\frac{703}{11}$ lunar days.

If we now multiply the number of *ûnarâtra* days, which corresponds to the number of lunar days by $63\frac{150.653}{353.739}$, the product is less than that which we get by multiplying by $63\frac{10}{11}$. If we, therefore, want to divide the lunar days by $\frac{703}{11}$, on the supposition that the quotient is equal to the first number, a certain portion must be added to the lunar days, and this portion he (the author of *Pulisa-Siddhânta*) had not computed accurately, but only approximatively. For if we multiply the universal *ûnarâtra* days by 703, we get the product 17,633,032,650,000, which is more than eleven times the universal lunar days. And if we multiply the universal lunar days by 11, we get the product 17,632,989,000,000.

The difference between the two numbers is 43,650,000. If we divide by this number the product of eleven times the universal lunar days, we get as quotient 403,963.

Criticisms of this method.

This is the number used by the inventor of the method. If there were not a small remainder beyond the last-mentioned quotient (403,963 + a fraction), his method would be perfectly correct. However, there remains a fraction of $\frac{405}{43651}$ or $\frac{9}{971}$, and this is the amount which is neglected. If he uses this divisor without the fraction, and divides by it the product of eleven times the partial lunar days, the quotient would be by so much larger as the dividendum has increased. The other details of the calculation do not require comment.

Method for finding the *adhimâsa* for the years of a *kalpa*, *caturyuga*, or *kaliyuga*.

Because the majority of the Hindus, in reckoning their years, require the *adhimâsa*, they give the preference to this method, and are particularly painstaking in describing the methods for the computation of the *adhimâsa*, disregarding the methods for the computation of the *ûnarâtra* days and the *sum of the days* (*ahargaṇa*). One of their methods of finding the *adhimâsa* for the years of a *kalpa* or *caturyuga* or *kaliyuga* is this:—

They write down the years in three different places. They multiply the upper number by 10, the middle by 2481, and the lower by 7739. Then they divide the middle and lower numbers by 9600, and the quotients are days for the middle number and *avama* for the lower number.

The sum of these two quotients is added to the number in the upper place. The sum represents the number of the complete *adhimâsa* days which have elapsed, and the sum of that which remains in the other two places is the fraction of the current *adhimâsa*. Dividing the days by 30, they get months.

Ya'ḳûb Ibn Ṭârik states this method quite correctly. We shall, as an example, carry out this computation for our gauge-year. The years of the *kalpa* which have elapsed